

SIMPLIFIED MEASUREMENTS

OF

THE HEAT TRANSFER COEFFICIENT

قياسات مبسطة لمعامل انتقال الحرارة

BY

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الخلاصة :

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 بواسطة استخدام الشريحة الرقيقة ، يمكن قياس التدفق الحراري خلال الحائط وكذلك درجات الحرارة على السطح التي بواسطتهم يمكن حساب معامل انتقال الحرارة وقد استخدم لهذا الغرض لوح من النحاس الاحمر معزول من احد الوجة ويسخن بواسطة مرور تيار كهربى خلاله . كما حققت النسبة بين قيمتى معامل رابلى ومربع معامل رسولدر دائما أقل من الواحد وذلك لتكون الحرارة المنتقلة من سطح لوح النحاس الى الهواء المجاور بواسطة الحمل الحر فقط . وفقدتم القياس للحالات التالية .
 ١ - اللوح النحاسى فى وضع رأسى والتسخين من ناحية واحدة
 ٢ - اللوح النحاسى فى وضع افقى والتسخين من الناحية العليا .
 ٣ - اللوح النحاسى فى وضع افقى والتسخين من الناحية السفلى .
 وقد تم حساب معامل انتقال الحرارة بالحمل فى الثلاث حالات السابقة بالقياس بواسطة الشريحة والأزدواج الحرارى من نوع نحاسى - كونسنتان .
 كما فورنت النتائج المعملية الحاصل عليها فى كل من حالتي القياس بواسطة الشريحة الرقيقة والأزدواج الحرارى مع النتائج النظرية السابقة الحاصل عليها بواسطة الباحثين فى هذا المجال وقد وجد ان النتائج الحاصل عليها بواسطة الشريحة هي الاكثر تطابقا مع النتائج التحليلية عنها فى حالة الأزدواج الحرارى . على الرغم انما من سهولة الاستخدام والقياس فى حالة الشريحة الرقيقة عنها فى حالة المزدوج الحرارى .

ABSTRACT- A micro-foil heat flow sensor is used to measure the heat flux and temperatures at a wall in order to determine the local heat transfer coefficient. An electrically heated copper plate is used for this purpose. The heat is considered to be transferred by free convection and the heat transfer coefficient can be calculated accordingly.

Three cases were studied:

- i. Vertical plate with one heated side
- ii. Horizontal plate with heated upper surface
- iii. Horizontal plate with heated lower surface.

The results obtained by the use of micro-foil sensor ..
 by the use of copper-constantan thermocouples were compared with results obtained theoretically by other investigators. Better agreement of heat transfer coefficients obtained by foil measurements and theoretical analysis than those by thermocouples measurements, although the technique of foil measurements is simpler.

INTRODUCTION

The micro-foil heat flow sensor is a differential thermocouple type sensor which utilizes a thin foil type thermopile bonded to both sides of a known thermal barrier as shown in Fig. 1. The temperature difference across the thermal barrier is proportional to the heat flow through the sensor.

The function of heat flow sensor is to measure heat transfer (loss or gain) through a surface. It differentiates between the temperatures of two opposite sides of certain rigid materials and thereby allowing a direct measurement of the heat loss or gain through the material surface. The heat flow sensor is cemented onto a surface like strain gauges. The sensor is very thin and flexible and can be attached to flat or curved surfaces without damage to these surfaces. No special wiring, reference junctions, or signal conditioning are required. Readout is accomplished by connecting the sensor to any direct reading microvoltmeter or recorder.

The goal of all convection heat transfer problems is to find the fluid temperature distribution as a function of geometry, flow conditions, and fluid properties. The wall heat transfer is found by applying Fourier's law of conduction for the thermal boundary layer next to the wall, i.e.;

$$q_w = -k \left. \frac{dt}{dy} \right|_{y=0} \quad (1)$$

The Newton's equation:

$$q_w = h (t_s - t_{\infty}) \quad (2)$$

is then used to find the heat transfer coefficient h .

If the temperature distribution of the fluid close to the wall, $t(y)$, cannot be found analytically, then q_w may be determined from experimental measurements. Micro-Foil technique can be used directly to measure the heat flux from a solid surface to a fluid and, consequently, the heat transfer coefficient is obtained by the use of Eq. 2.

For reasons of economy or scale, many engineering problems are concerned solely with free convection for example, cooling of electronic devices or domestic baseboard water and steam heaters. Even in designs of forced flow systems (e.g. pressurized water reactors), calculation of heat transfer by free convection is necessary for safety and protection considerations against burnout if the power moving the forced streams should fail. Finally, in geophysical problems, free convection is the dominant mode of heat transfer: atmospheric and oceanic motions are dominated by massive natural convection effects arising from special and temporal variations of solar heating. Therefore, the natural convection mode is chosen to check the validity of micro-foil measurements.

EXPERIMENTAL RIG AND APPARATUS:

Figure 2 shows the used experimental rig and the measuring instruments. The rig test section is a copper plate of 457.2 mm height x 254 mm width x 0.035 mm thickness. The copper plate is clad with a mica plate of 2.11 mm thickness. Then the copper plate is divided to eighteen strips of 24.4 mm width each. The grooves between strips (of 1 mm width) are filled with mastic plaster, and sanded-off by smooth sand paper to utilize the copper plate as an electrical heater, see Fig. 2. The electric current passes through those serial strips to heat the copper plate. The electrical power supply is determined from the measurements of the potential voltage between the ends of the electrically heated copper plate by a voltmeter (kept constant at 1.95 volts). The electric resistance of the plate can

be calculated by;

$$R = \frac{\rho_e L}{A} = \frac{1.6 \times 10^{-8} \times 0.254 \times 18}{0.0244 \times 0.035 \times 10^{-3}} = 0.086 \text{ ohm}$$

The electrical power for heating is ;

$$Q = \frac{V^2}{R} = \frac{(1.95)^2}{0.086} = 44.39 \text{ Watts.}$$

As the plate surface area is 0.116 m^2 ($0.457 \text{ m} \times 0.254 \text{ m}$), then the electric heating per unit area is ;

$$q_e = \frac{Q}{A} = \frac{44.39}{0.116} = 382.68 \text{ W/m}^2$$

The surface temperature (kept at less than $55 \text{ }^\circ\text{C}$) is measured by copper-constantan thermocouple. The ambient room temperature is also recorded by a copper-constantan thermocouple. The heat loss.. by radiation from the copper plate is estimated by considering the emissivity of the polished copper is 0.045 and ambient temperature of $22 \text{ }^\circ\text{C}$, by;

$$q_r = \epsilon E [(T_s)^4 - (T_\infty)^4] \\ = 0.045 \times 5.6695 \times 10^{-8} [(55 + 273)^4 - (22 + 273)^4] = 10.21 \text{ W/m}^2$$

Therefore, the heat loss.. by radiation can't be neglected, and should be include-in the calculation of heat transfer coefficient.

The mica plate is also covered by plywood plate 12.5 mm in thickness. Then the thermal properties of the heated plate are:

a) For Copper

$$\begin{aligned} \rho &= 8890 \text{ kg/m}^3 \\ C_p &= 385.4 \text{ J/kg K} \\ \alpha &= 11.24 \times 10^{-5} \text{ m}^2/\text{S} \\ k &= 385 \text{ W/mK} \\ x &= 0.035 \text{ mm} \end{aligned}$$

b) For Mica

$$\begin{aligned} k &= 0.035 \text{ W/mK} \\ x &= 2.11 \text{ mm} \end{aligned}$$

c) For Plywood

$$\begin{aligned} k &= 0.12 \text{ W/mK} \\ x &= 12.5 \text{ mm} \end{aligned}$$

The thermal resistance of the heated plate may be calculated by:

$$R_t = \left(\frac{x}{k}\right)_c + \left(\frac{x}{k}\right)_m + \left(\frac{x}{k}\right)_w$$

The heat loss by conduction from the mica side can be calculated by:

$$q_c = \frac{t_s - t_2}{R_t}$$

where, t_2 is the plywood surface temperatures, and is measured by using a copper-constantan thermocouple. Therefore, the heat loss by conduction is computed to be 19.5 W/m^2 , for t_2 equal to $51.8 \text{ }^\circ\text{C}$.

Then the heat transferred by convection is estimated by subtracting the summation of heat losses by radiation and conduction from the generated heat by electricity, i.e.

$$\begin{aligned} q_w &= q_e - (q_r + q_c) \\ &= 382.68 - (10.21 + 19.5) = 352.97 \text{ W/m}^2 \end{aligned}$$

The micro-foil heat flow sensor was used to simplify the measurement of heat flux. The completed sensor was placed in intimate contact with the copper plate surface where the heat transfer rates are to be measured. The same energy passes through both the surface and the sensor attached with it. The thermal energy passes through a material, in this case the barrier due to the existence of a temperature gradient Δt . This temperature gradient is directly proportional to the magnitude of the thermal energy or, more precisely, the heat transfer rate.

The technical data of the used heat flow sensor (Rdf Corporation type 20457-1) are:

| | |
|--|--|
| i) Calibrated sensitivity at $21 \text{ }^\circ\text{C}$ | = $0.393 \mu\text{v/w/m}^2$ |
| ii) Electrical resistance | = 100 ohm |
| iii) Nominal thickness | = 0.102 mm |
| iv) Heat capacity | = $204 \text{ J/m}^2 \cdot \text{ }^\circ\text{C}$ |
| v) Thermal resistance | = $0.0005 \text{ }^\circ\text{C/W/m}^2$ |
| vi) Emissivity of the micro-foil | = 0.05 |

Therefore, the heat flux can be directly measured by the heat flow sensor, and subtract the heat losses by radiation from the micro-foil, and the value is found equal to 353.66 W/m^2 . This value is close to the other value, which is calculated by using the thermocouple.

RESULTS AND DISCUSSION:

Figure 3 indicates the surface temperature and heat flux versus the time for the heated vertical plate. The surface temperatures were measured by both micro-foil sensor and the copper-constantan thermocouple. The temperatures measured by both methods were plotted and showed good agreement. However, the values of the surface temperature as measured by the micro-foil sensor were found higher than those values obtained by the thermocouple measurements. The reason is the different positions of the temperature sensing elements of both methods. The sensing element of the micro-foil is buried under the foil itself, while the thermocouple is bonded to the plate surface. It should be noted here that the steady state condition was reached within thirty minutes after energising starts, and recorded temperature difference is $35 \text{ }^\circ\text{C}$.

The values of the heat flux measured by the micro-foil were found lower than supplied electrical energy, because of the heat losses, by radiation and conduction in the last one.

Sparrow and Gregg (1) recommended the following equation for laminar free convection from a vertical plate with constant heat flux:

$$Nu_L = 0.59 (Gr_L Pr)^{1/4} \text{ for } 10^3 < Gr_L Pr < 10^4 \quad (3)$$

The heat transfer coefficients calculated by Equation 3, were plotted in Fig. 4, together with those obtained from the micro-foil sensor measurements. The values of heat transfer coefficient obtained experimentally are higher than those calculated theoretically [Ref.1]. The experimental values of the heat transfer coefficients depend on the electric current value passing through the copper plate cross-section. While the calculated theoretical values depend on the fluid properties and plate dimensions. However, similar trend is obtained between the values obtained by both methods as shown in Fig. 4. Poor agreement was found between the data obtained by the copper-constantan thermocouple measurements and theoretical data obtained by [Ref.1].

Figures 5 and 7 show the surface temperature and heat flux versus the time for horizontal plate heated upward, and downward respectively. The steady state conditions was reached for lower heated surface case in shorter time than that for the upper heated surface. The figures also show the measurements obtained by the thermocouple are higher than those obtained by the micro-foil for the same reason mentioned earlier.

Figures 6 and 8 show the heat transfer coefficient values versus the temperature difference, for horizontal plates heated upward, and downward surface respectively. The measurements obtained by both micro-foil sensor and copper constantan thermocouple are compared with the following results:

i) For horizontal plate with upper heated surface [See Ref.2].

$$Nu_L = 0.15 (Ra_L)^{1/3} \quad (4)$$

ii) For horizontal plate with lower heated surface [See Ref.3]:

$$Nu_L = 0.27 (Ra_L)^{1/4} \quad (5)$$

where, L is the characteristic length and can be represented by the average of the sum of length and width of the rectangular plate.

The same trend was shown between the result obtained by the micro-foil and theoretical data (See Figs. 6 and 8). Poor agreement is observed for the results obtained by copper-constantan thermocouple measurements and theoretical calculations as shown in Figs.6 and 8.

CONCLUSION:

- 1- Heat flux can be simply and more accurately measured by using the micro-foil technique as compared with thermocouples measurements.
- 2- The measurements obtained by the micro-foil agree closely with the calculations obtained theoretically
- 3- Poor agreement was observed between the results obtained by the copper-constantan thermocouple and theoretical calculations.

- 4- The surface temperature readings by using the micro-foil sensor or copper-constantan thermocouple are found in good agreement, while the heat transfer coefficients calculated by both micro-foil and thermo couple are found in poor agreement.
- 5- Stability of measurements by using the micro-foil is attained within 30 minutes.
- 6- Micro-foil sensor may be simple to use it in different applications.

NOMENCLATURE:

| | |
|-------------------|---|
| A, a | = Surface area, and cross-section area, (m^2) |
| B | = Width of copper plate, (m) |
| C_p | = Specific heat of fluid at constant pressure ($J/kg \text{ } ^\circ C$) |
| h | = Heat transfer coefficient, ($W/m^2 \text{ } ^\circ C$) |
| k | = Thermal conductivity, ($W/m \text{ } ^\circ C$) |
| L | = Length of plate, (m) |
| Q | = Electric heating, (W) |
| q_w, q_e | = Heat flux, and electric heating per unit area, (W/m^2) |
| q_r, q_c | = Heat losses by radiation, and conduction (W/m^2) |
| R, R_t | = Electric resistance (ohm), and thermal resistance (mk/W) |
| $T \text{ \& } t$ | = Absolute temperature, (K) and centigrade temperature, ($^\circ C$) |
| U | = Free stream velocity, (m/s) |
| V | = Electric potential, (volt) |
| x | = Thickness of plate, (m) |
| y | = Normal to the wall, (m) |
| α | = Thermal diffusivity, ($k / \rho c$) (m^2/s) |
| β | = Thermal expansion coefficient, (P / k) |
| μ | = Viscosity, (Kg/ms) |
| ν | = Kinematic viscosity, (m^2/s) |
| ρ, ρ_e | = Density, (kg/m^3), and specific electric resistance of copper, ($= 1.6 \times 10^{-8}$ ohm. m) |
| σ | = Stefan-Boltzmann constant ($= 5.6695 \times 10^{-8} W/m^2 k^4$) |
| ϵ | = Emissivity of copper |
| G_L | = Grashof number ($= g\beta(T_s - T_\infty) L^3 / \nu^2$) |
| N_{uL} | = Nusselt number, ($h L / k_f$) |
| P_{rL} | = Prandtl number, ($= \mu C_p / k_f$) |
| R_{aL} | = Rayleigh number, ($= G_{rL} P_{rL}$) |
| R_e | = Reynolds number, ($= \rho u_\infty L / \mu$) |

Subscripts

| | |
|----------|-------------------------------------|
| f | = of the fluid |
| c | = copper |
| w | = plywood |
| s | = wall surface |
| x | = in the x-direction |
| m | = mica |
| ∞ | = ambient or freestream conditions. |

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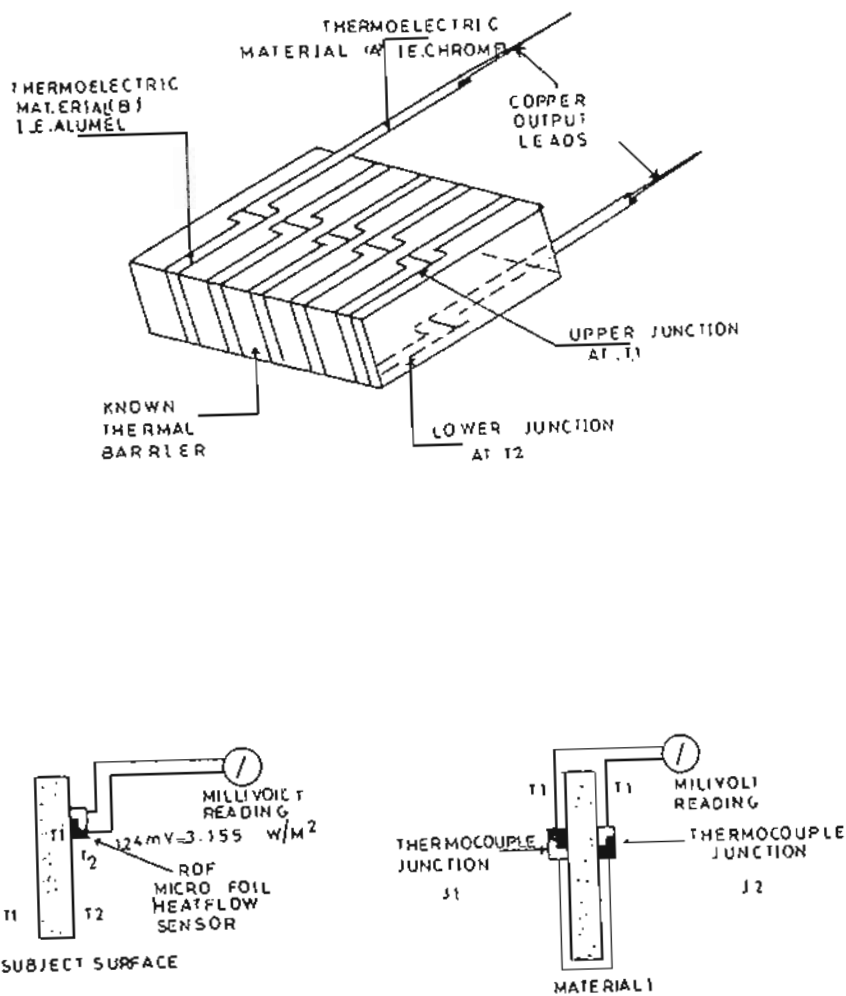


FIG 1 HEAT FLOW SENSOR

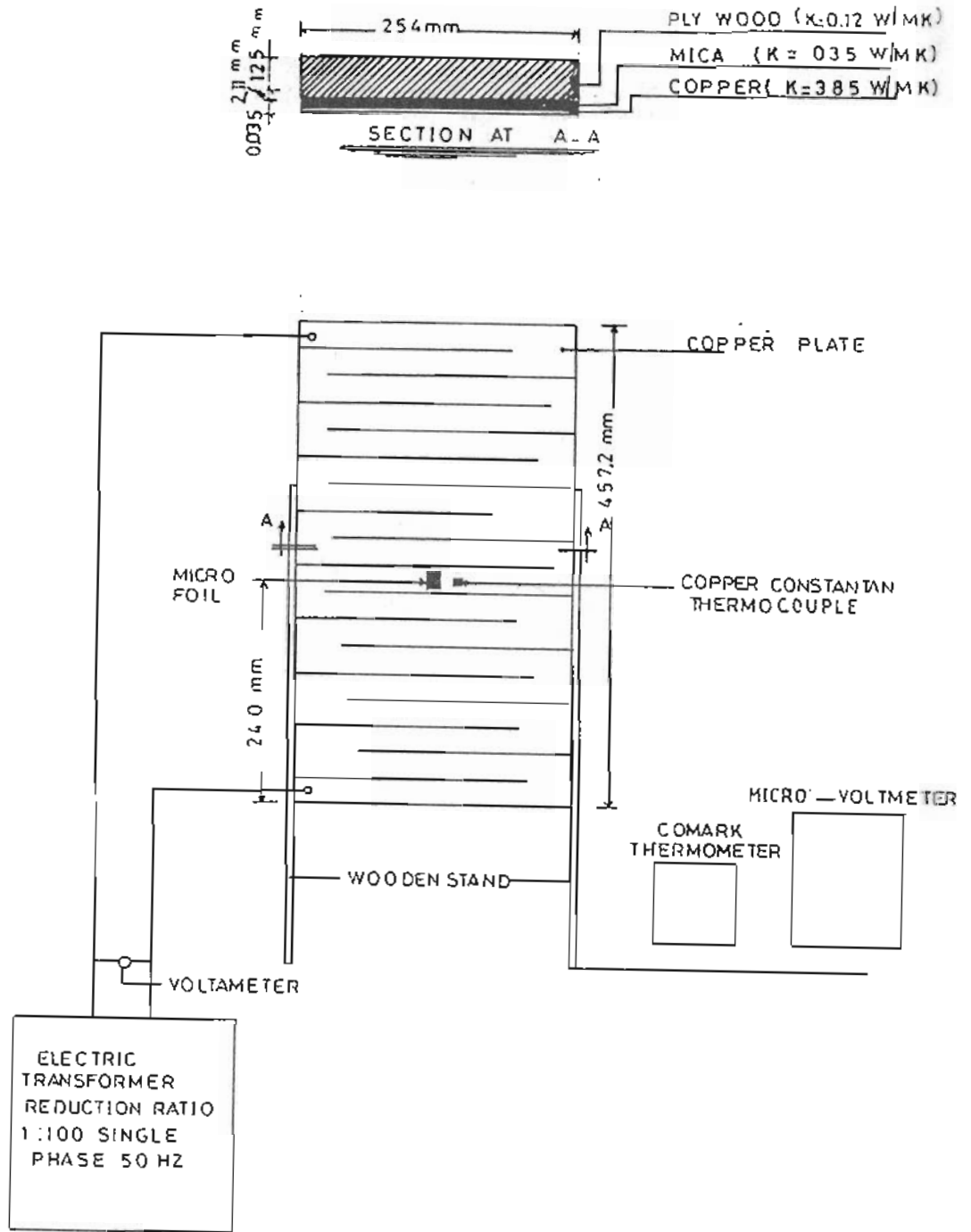


FIG 2 EXPERIMENTAL RIG ARRANGEMENT

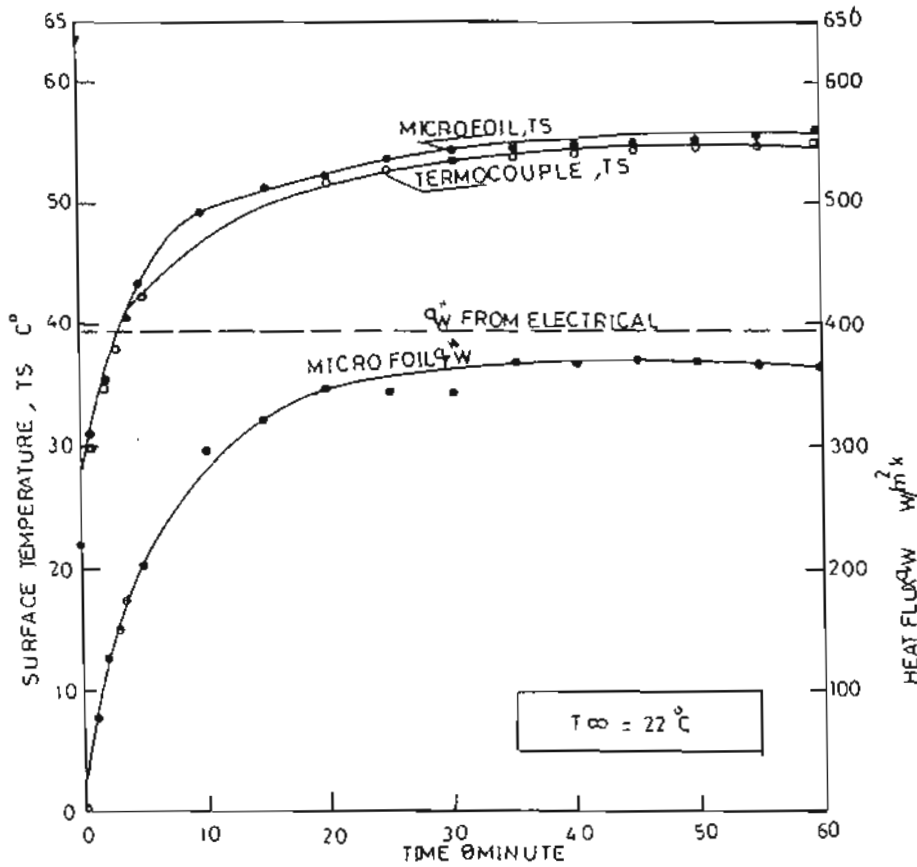


FIG3 SURFACE TEMPERATURE AND HEAT FLUX FOR A VERTICAL PLATE

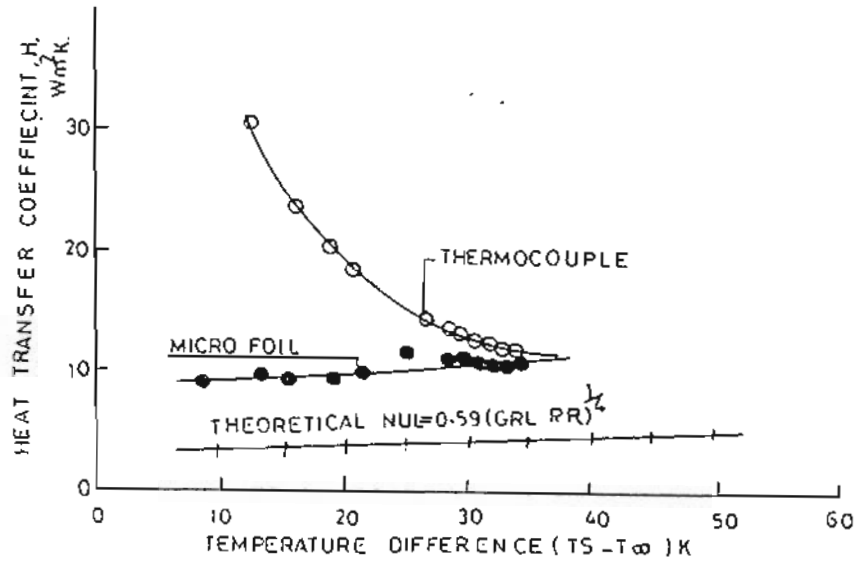


FIG 4 HEAT TRANSFER COEFFICIENT FOR A VERTICAL PLATE

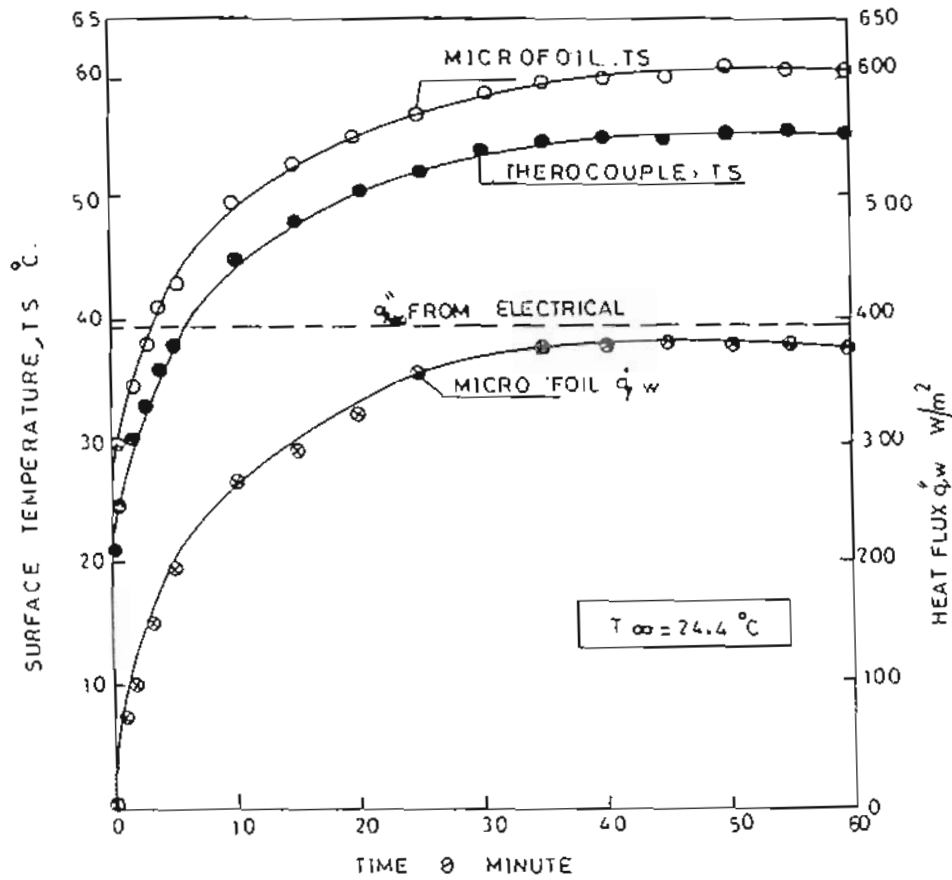


FIG 5 SURFACE TEMPERATURE AND HEAT FLUX FOR A HORIZONTAL PLATE WITH UPPER SURFACE HEATED

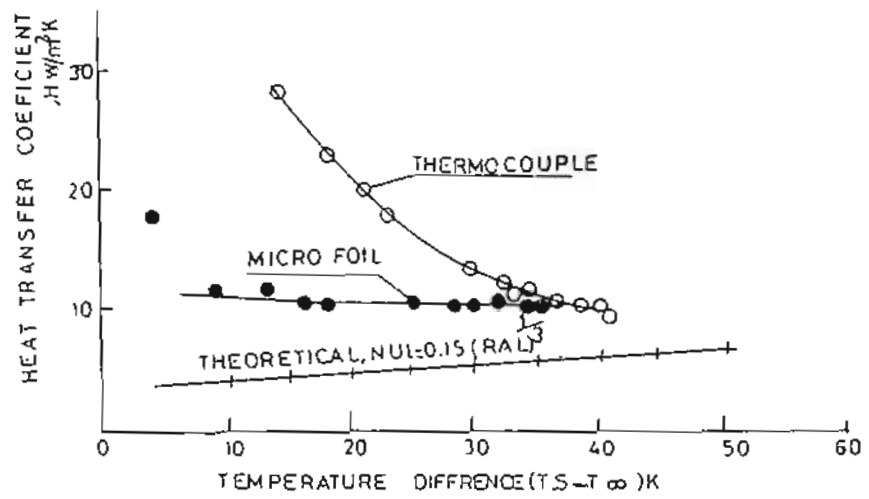


FIG 6 HEAT TRANSFER COEFFICIENT FOR A HORIZONTAL PLATE WITH UPPER SURFACE HEATED

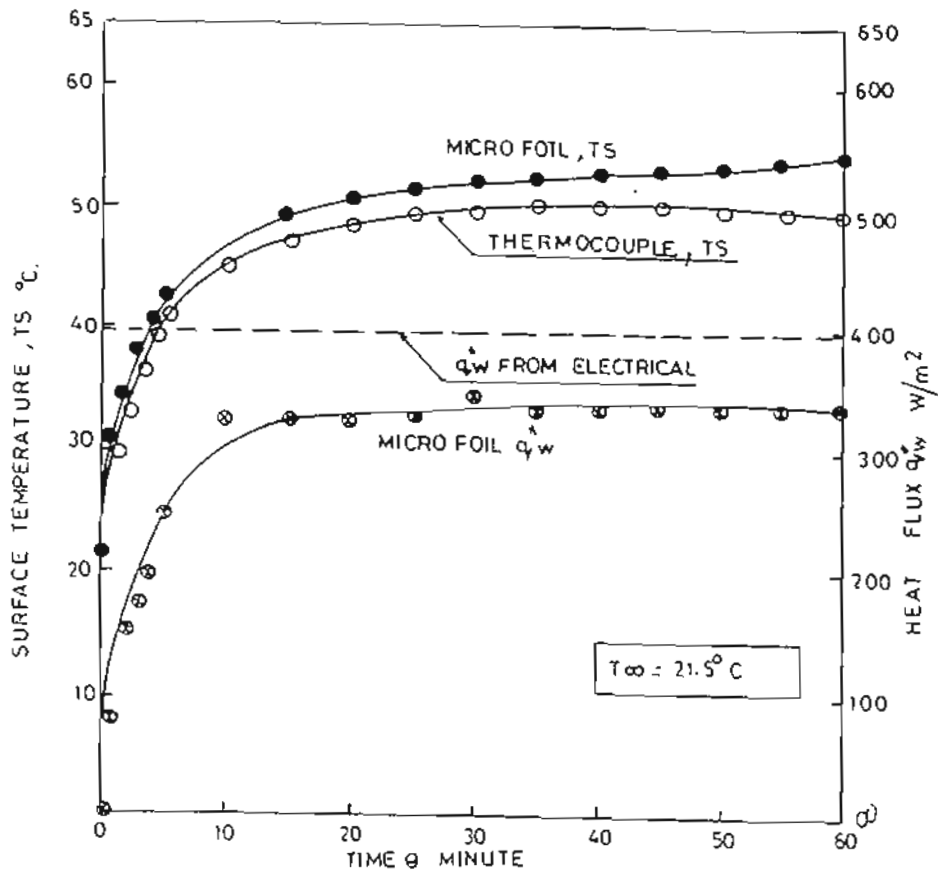


FIG.7 SURFACE TEMPERATURE AND HEAT FLUX FOR HORIZONTAL PLATE LOWER SURFACE HEATED

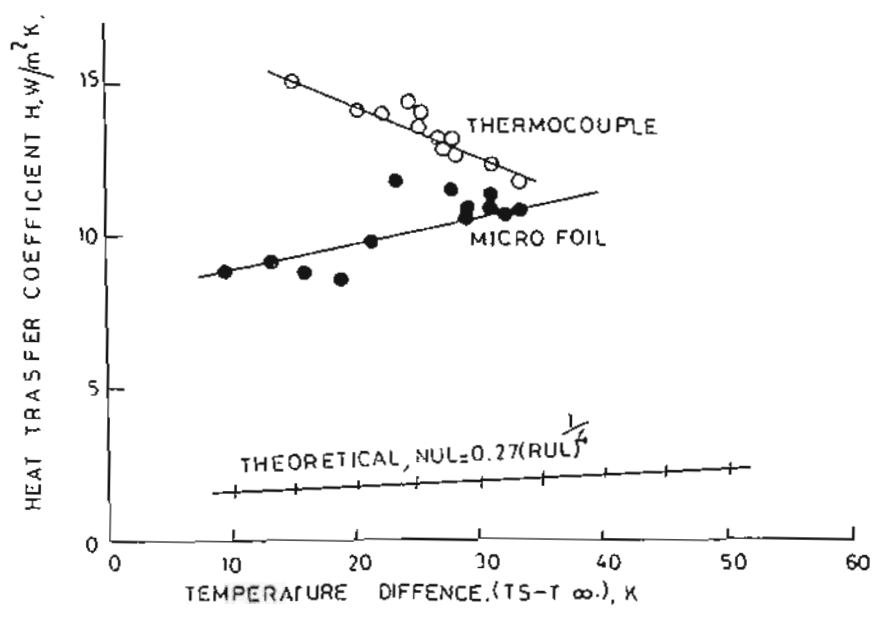


FIG 8 HEAT TRANSFER COEFFICIENT FOR HORIZONTAL PLATE WITH LOWER SURFACE HEATED