



Open Book Exam

Attempt all questions. Assume any missed data. Full mark is 100

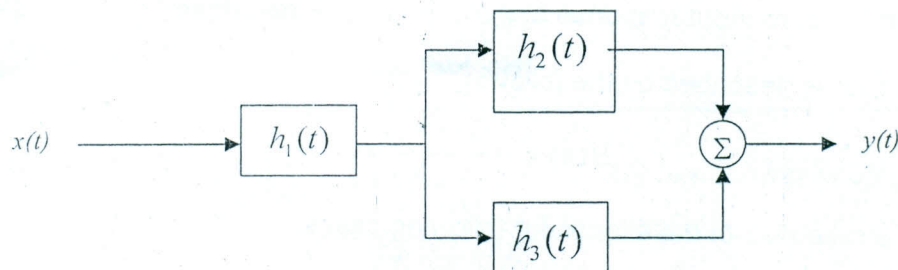
Q.1.a) Correct the errors, if any, in each of the following statements [10 Marks]

- i. The system described by $h(n) = 3^n u(n)$ is stable.
- ii. The system described by $y(n) = anx^2(n)$ is time invariant.
- iii. The signal $x(t) = u(t - 2)$ is a power signal.
- iv. The system described by $y = 2x + 3$ is linear.
- v. The system described by $h(t) = -\delta(-t) + \delta(3t)$ is memoryless.
- vi. The signal $x(n) = \sin 2n + \cos 4n$ is periodic with fundamental period π .
- vii. The signal $x(n) = \cos \Omega_0 n u(n)$ is periodic.
- viii. Any continuous-time signal, $x(t)$, can have Fourier series representation.
- ix. In distortionless transmission, both amplitude and phase of the frequency response must be constant over the entire frequency rang.
- x. A signal is band-limited if $|X(\omega)| = 0$ for $|\omega| < \omega_M$

Q.1.b) An interconnection of LTI system is shown below. The impulse responses are:

$$h_1(t) = 2u(t - 1) - 2u(t - 3), \quad h_2(t) = \delta(t) - \delta(t - 2), \quad h_3(t) = \delta(t - 1) + \delta(t - 2)$$

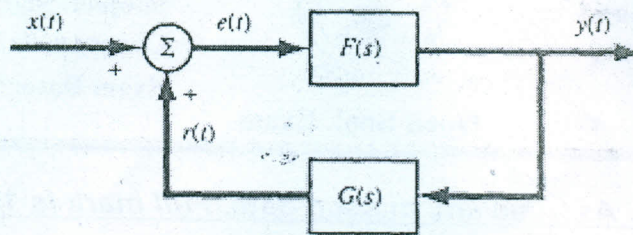
- i. Express the impulse response of the overall system, $h(t)$, in terms of $h_1(t)$, $h_2(t)$, and $h_3(t)$. Evaluate $h(t)$ and determine whether the system corresponding to $h(t)$ is stable and causal.
- ii. If $x(t) = 2\delta(t - 4)$, find the output, $y(t)$. [10 Marks]



Q.2.a) For the transfer function $H(s) = \frac{s + 2}{s^2 + 4s - 5}$

- i. Sketch the pole-zero plot for this transfer function.
- ii. What are the possible ROC's for this transfer function?
- iii. For each ROC in (ii), determine stability and causality of the system
- iv. For each ROC in (ii), determine the associated inverse transform. [10 Marks]

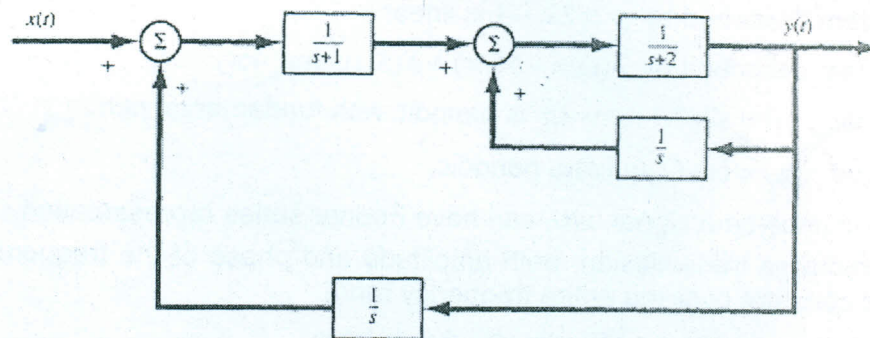
Q.2.b) The feedback interconnection of two causal subsystems with system functions $F(s)$ and $G(s)$ is depicted in the shown figure. [10 Marks]



Show that the overall system function $H(s)$ for this feedback system is given by:

$$H(s) = \frac{F(s)}{1 - F(s)G(s)}$$

Use the result to determine the overall system function $H(s)$ for the system shown below.



Q.3.a) Consider an LTI system described by the differential equation

$$y''(t) - 4y(t) = x(t), \quad y(0) = 1, \quad y'(0) = 1$$

- Find the system function. Locate poles and zeros in the s-plane.
- Find the impulse response of the system.
- Find the output of the system if $x(t) = u(t)$.
- What are the zero-input response and the zero-state response?

[10 Marks]

Q.3.b) A digital filter is described by the following system function:

$$H(z) = \frac{z(z-1)}{z^2 - 2.5z + 1}$$

Find the impulse response of the filter in the following cases:

- $|z| > 2$
- $|z| < 0.5$

In each case, verify the first three terms of your answer using power series expansion method. [10 Marks]

Q.4.a) Consider a system described by

$$y(n) - 3y(n-1) = x(n), \quad y(-1) = 1, \quad x(n) = 4u(n)$$

- Find the system function and locate its poles and zeros in the complex plane.
- Determine the output of the system.
- Express the output $y(n)$ as a sum of two components; the zero-state response and the zero-input response. [10 Marks]

Q.4.b) Consider a periodic square wave $x(t)$ given by:

$$x(t) = \begin{cases} 10 & 0 \leq t \leq 2 \\ 0 & 2 \leq t \leq 4 \end{cases}, \quad x(t) = x(t + 4)$$

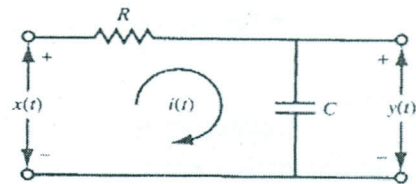
- Sketch $x(t)$. State the conditions required for the convergence of Fourier series.
- Find the trigonometric Fourier series of $x(t)$.
- If $x(t)$ is applied as an input to a high-pass filter with frequency response

$$H(\omega) = \begin{cases} 1 & |\omega| \geq 8\pi \\ 0 & |\omega| < 8\pi \end{cases}$$

Find the output of the filter.

[10 Marks]

Q.5.a) Derive an expression for the frequency response of the shown circuit. Sketch the magnitude and phase of the frequency response. Indicate the cut-off frequency on your sketch. Choose suitable values for R and C to realize a cut-off frequency of 10KHz. [5 Marks]



Q.5.b) A system is described by the frequency response

$$H(\omega) = \begin{cases} e^{-j\pi/4} & |\omega| < \pi/3 \\ 0 & |\omega| > \pi/3 \end{cases}$$

- Determine the impulse response $h(t)$ of this filter.
- Calculate the output of the system if the i/p is $x(t) = \cos(\frac{\pi}{6}t + 0.4\pi)$ [5 Marks]

Q.5.c) Sketch the Bode plot for the following frequency response

$$H(\omega) = \frac{1000(1 + j\omega)}{j\omega(100 + j\omega)} \quad [10 Marks]$$

My best wishes to all of you!

Assis. Prof. Hossam EL-Din Moustafa