



Allowed Tables and Charts: None

Answer all the following questions (with neat sketches)

Question (1)

(50 Marks)

- A. Explain with neat sketches the following terms:
Length scale, Energy cascade, Energy backscatter, Two-point correlation. **(8 Marks)**
- B. For a boundary layer flow, derive the momentum integral equation of von Kármán, in which the momentum thickness Θ and displacement thickness δ_1 are related to the wall shear stress τ_w with the presence of pressure gradient and free-stream velocity U_∞ as the following relation:
$$\frac{d\Theta}{dx} + \frac{(2\Theta + \delta_1)}{U_\infty} \frac{\partial U_\infty}{\partial x} = \frac{\tau_{wall}}{\rho U_\infty^2}$$
 (18 Marks)
- C. Derive the growth of the turbulent boundary layer thickness, the displacement thickness, the momentum thickness and the wall skin friction coefficient of a turbulent flow over a flat plate (without pressure gradient). How do you compute the total drag force of the plate? **(14 Marks)**
- D. Discuss the different regions in the boundary layer. Write the law of the wall, from which how do you derive the Clauser's plot relation? **(10 Marks)**

Question (2)

(50 Marks)

- A. For 3-dimensional incompressible flow develop the continuity and Navier-Stokes equations in Cartesian coordinates. Reduce the final forms to steady incompressible flow. **(20 Marks)**
- B. Explain how to develop the turbulent Reynolds-stresses tensor matrix in three-dimensional turbulent flow. **(15 Marks)**
- C. Give a brief outline of the Blasius solution of laminar boundary layer for flow over a flat plate in the form: $f f'' + 2 f''' = 0$. What are the boundary conditions from which the analytical solution can be developed. Write the function of the boundary layer and displacement thicknesses developing in streamwise direction. **(15 Marks)**

Best wishes
Professor Wageeh El-Askary